

General Certificate of Education  
January 2006  
Advanced Subsidiary Examination



**MATHEMATICS**  
**Unit Mechanics 1B**

**MM1B**

Monday 16 January 2006 9.00 am to 10.30 am

**For this paper you must have:**

- an 8-page answer book
  - the **blue** AQA booklet of formulae and statistical tables
- You may use a graphics calculator.

Time allowed: 1 hour 30 minutes

**Instructions**

- Use blue or black ink or ball-point pen. Pencil should only be used for drawing.
- Write the information required on the front of your answer book. The *Examining Body* for this paper is AQA. The *Paper Reference* is MM1B.
- Answer **all** questions.
- All necessary working should be shown; otherwise marks for method may be lost.
- The **final** answer to questions requiring the use of calculators should be given to three significant figures, unless stated otherwise.
- Take  $g = 9.8 \text{ m s}^{-2}$ , unless stated otherwise.

**Information**

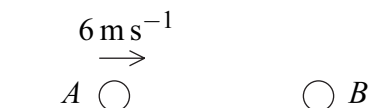
- The maximum mark for this paper is 75.
- The marks for questions are shown in brackets.
- Unit Mechanics 1B has a **written paper only**.

**Advice**

- Unless stated otherwise, formulae may be quoted, without proof, from the booklet.

Answer **all** questions.

- 1 A particle  $A$  moves across a smooth horizontal surface in a straight line. The particle  $A$  has mass  $2\text{ kg}$  and speed  $6\text{ m s}^{-1}$ . A particle  $B$ , which has mass  $3\text{ kg}$ , is at rest on the surface. The particle  $A$  collides with the particle  $B$ .



- (a) If, after the collision,  $A$  is at rest and  $B$  moves away from  $A$ , find the speed of  $B$ .  
(3 marks)
- (b) If, after the collision,  $A$  and  $B$  move away from each other with speeds  $v\text{ m s}^{-1}$  and  $4v\text{ m s}^{-1}$  respectively, as shown in the diagram below, find the value of  $v$ .



- 2 A particle  $P$  moves with acceleration  $(-3\mathbf{i} + 12\mathbf{j})\text{ m s}^{-2}$ . Initially the velocity of  $P$  is  $4\mathbf{i}\text{ m s}^{-1}$ .

- (a) Find the velocity of  $P$  at time  $t$  seconds. (2 marks)
- (b) Find the speed of  $P$  when  $t = 0.5$ . (3 marks)

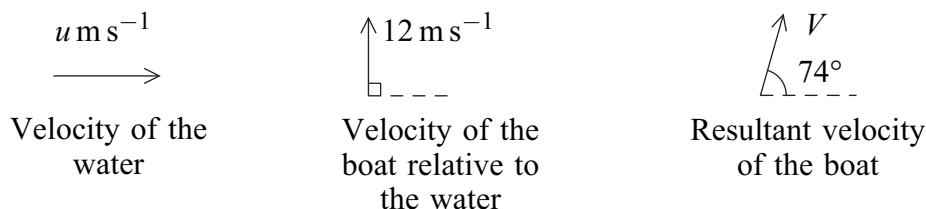
- 3 (a) A small stone is dropped from a height of  $25$  metres above the ground.

- (i) Find the time taken for the stone to reach the ground. (2 marks)
- (ii) Find the speed of the stone as it reaches the ground. (2 marks)

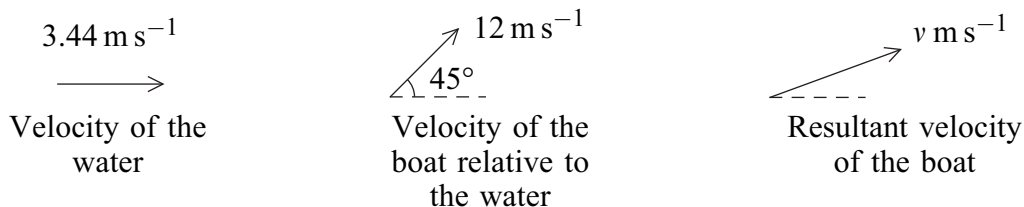
- (b) A large package is dropped from the same height as the stone. Explain briefly why the time taken for the package to reach the ground is likely to be different from that for the stone. (2 marks)

4 Water flows in a constant direction at a constant speed of  $u \text{ m s}^{-1}$ . A boat travels in the water at a speed of  $12 \text{ m s}^{-1}$  relative to the water.

- (a) The direction in which the boat travels relative to the water is perpendicular to the direction of motion of the water. The resultant velocity of the boat is  $V \text{ m s}^{-1}$  at an angle of  $74^\circ$  to the direction of motion of the water, as shown in the diagram.



- (i) Find  $V$ . (2 marks)
- (ii) Show that  $u = 3.44$ , correct to three significant figures. (3 marks)
- (b) The boat changes course so that it travels relative to the water at an angle of  $45^\circ$  to the direction of motion of the water. The resultant velocity of the boat is now of magnitude  $v \text{ m s}^{-1}$ . The velocity of the water is unchanged, as shown in the diagram below.

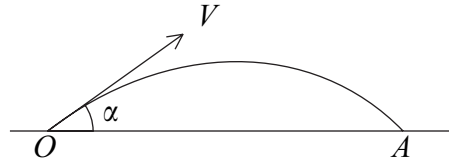


Find the value of  $v$ . (4 marks)

**Turn over for the next question**

**Turn over** ►

- 5 A golf ball is projected from a point  $O$  with initial velocity  $V$  at an angle  $\alpha$  to the horizontal. The ball first hits the ground at a point  $A$  which is at the same horizontal level as  $O$ , as shown in the diagram.



It is given that  $V \cos \alpha = 6u$  and  $V \sin \alpha = 2.5u$ .

- (a) Show that the time taken for the ball to travel from  $O$  to  $A$  is  $\frac{5u}{g}$ . (4 marks)
- (b) Find, in terms of  $g$  and  $u$ , the distance  $OA$ . (2 marks)
- (c) Find  $V$ , in terms of  $u$ . (2 marks)
- (d) State, in terms of  $u$ , the least speed of the ball during its flight from  $O$  to  $A$ . (1 mark)

6 A van moves from rest on a straight horizontal road.

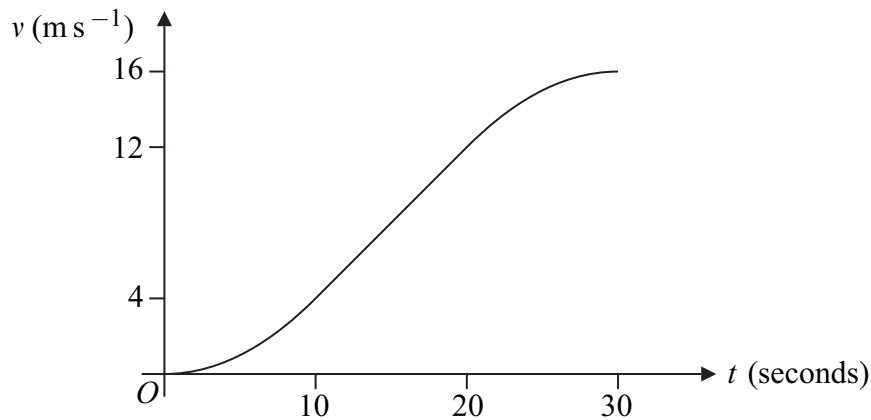
- (a) In a simple model, the first 30 seconds of the motion are represented by three separate stages, each lasting 10 seconds and each with a constant acceleration.

During the first stage, the van accelerates from rest to a velocity of  $4 \text{ m s}^{-1}$ .

During the second stage, the van accelerates from  $4 \text{ m s}^{-1}$  to  $12 \text{ m s}^{-1}$ .

During the third stage, the van accelerates from  $12 \text{ m s}^{-1}$  to  $16 \text{ m s}^{-1}$ .

- (i) Sketch a velocity–time graph to represent the motion of the van during the first 30 seconds of its motion. (3 marks)
  - (ii) Find the total distance that the van travels during the 30 seconds. (4 marks)
  - (iii) Find the average speed of the van during the 30 seconds. (2 marks)
  - (iv) Find the greatest acceleration of the van during the 30 seconds. (2 marks)
- (b) In another model of the 30 seconds of the motion, the acceleration of the van is assumed to vary during the first and third stages of the motion, but to be constant during the second stage, as shown in the velocity–time graph below.

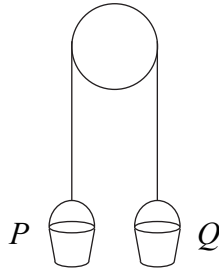


The velocity of the van takes the same values at the beginning and the end of each stage of the motion as in part (a).

- (i) State, with a reason, whether the distance travelled by the van during the first 10 seconds of the motion in **this** model is greater or less than the distance travelled during the same time interval in the model in part (a). (2 marks)
- (ii) Give one reason why **this** model represents the motion of the van more realistically than the model in part (a). (1 mark)

Turn over ►

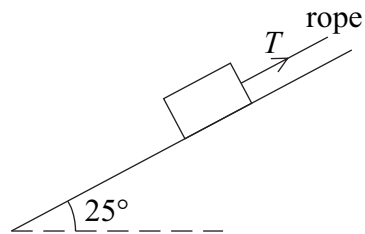
- 7 A builder ties two identical buckets,  $P$  and  $Q$ , to the ends of a light inextensible rope. He hangs the rope over a smooth beam so that the buckets hang in equilibrium, as shown in the diagram.



The buckets are each of mass  $0.6\text{ kg}$ .

- (a) (i) State the magnitude of the tension in the rope. *(1 mark)*
- (ii) State the magnitude and direction of the force exerted on the beam by the rope. *(2 marks)*
- (b) The bucket  $Q$  is held at rest while a stone, of mass  $0.2\text{ kg}$ , is placed inside it. The system is then released from rest and, in the subsequent motion, bucket  $Q$  moves vertically downwards with the stone inside.
- (i) By forming an equation of motion for each bucket, show that the magnitude of the tension in the rope during the motion is  $6.72\text{ newtons}$ , correct to three significant figures. *(6 marks)*
- (ii) State the magnitude of the force exerted on the beam by the rope while the motion takes place. *(1 mark)*

- 8 A rough slope is inclined at an angle of  $25^\circ$  to the horizontal. A box of weight 80 newtons is on the slope. A rope is attached to the box and is parallel to the slope. The tension in the rope is of magnitude  $T$  newtons. The diagram shows the slope, the box and the rope.



- (a) The box is held in equilibrium by the rope.
- Show that the normal reaction force between the box and the slope is 72.5 newtons, correct to three significant figures. *(3 marks)*
  - The coefficient of friction between the box and the slope is 0.32. Find the magnitude of the maximum value of the frictional force which can act on the box. *(2 marks)*
  - Find the least possible tension in the rope to prevent the box from moving down the slope. *(4 marks)*
  - Find the greatest possible tension in the rope. *(3 marks)*
  - Show that the mass of the box is approximately 8.16 kg. *(1 mark)*
- (b) The rope is now released and the box slides down the slope. Find the acceleration of the box. *(3 marks)*

**END OF QUESTIONS**

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